

Lesson 7-3

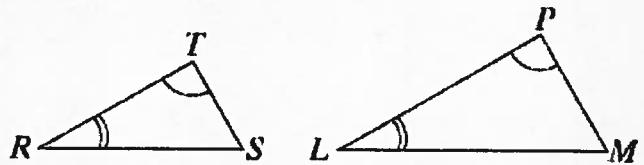
Proving Triangles Similar

Vocabulary and Key Concepts

Postulate 7-1: Angle-Angle Similarity (AA~) Postulate

If two angles of one triangle are congruent to two angles of another triangle, then the triangles are similar.

$$\triangle TRS \sim \triangle \boxed{PLM}$$

**Theorem 7-1: Side-Angle-Side Similarity (SAS~) Theorem**

If an angle of one triangle is congruent to an angle of a second triangle, and the sides including the two angles are proportional, then

the two triangles are similar

Theorem 7-2: Side-Side-Side Similarity (SSS~) Theorem

If the corresponding sides of two triangles are proportional, then

the two triangles are similar

Examples

- ① Using the AA~ Postulate $\overline{MX} \perp \overline{AB}$. Explain why the triangles are similar. Write a similarity statement.

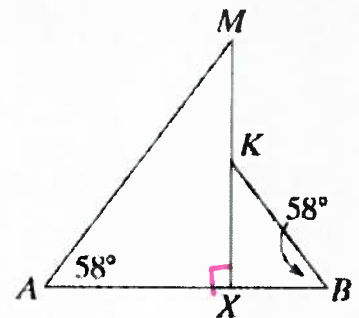
Because $\overline{MX} \perp \overline{AB}$, $\angle AXM$ and $\angle B XK$ are

$\boxed{\text{Right angles}}$, so $\angle AXM \cong \angle \boxed{B XK}$.

$\angle A \cong \angle \boxed{B}$ because their measures are equal.

$\triangle AMX \sim \triangle BKX$

by the $\boxed{AA\sim}$ Postulate.



- ② **Using Similarity Theorems** Explain why the triangles must be similar. Write a similarity statement.

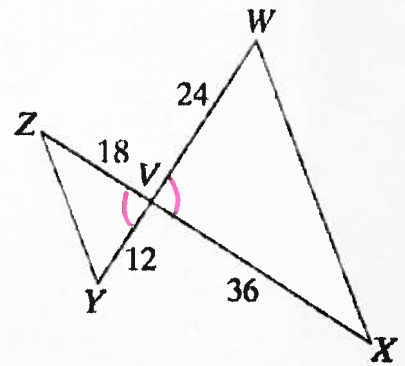
$\angle YVZ \cong \angle WVX$ because VAT

$$\frac{VY}{VW} = \frac{12}{24} = \frac{1}{2} \quad \text{and} \quad \frac{VZ}{VX} = \frac{18}{36} = \frac{1}{2}$$

so corresponding sides are proportional.

Therefore, $\triangle YVZ \sim \triangle WVX$

by the SAS ~ Theorem.

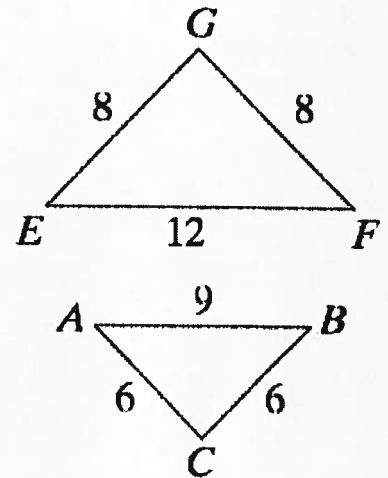


Explain why the triangles at the right must be similar.

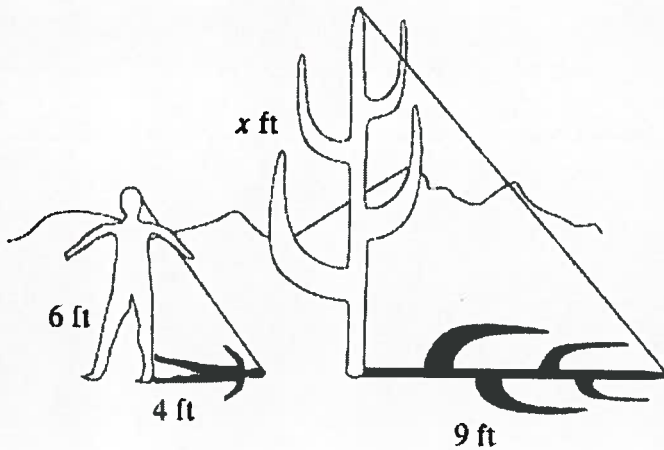
Write a similarity statement.

$\frac{12}{9} = \frac{4}{3} \checkmark$ $\frac{8}{6} = \frac{4}{3} \checkmark$ Sides are proportional

$\triangle EFG \sim \triangle ABC \rightarrow SSS \sim$



3. In sunlight, a cactus casts a 9-ft shadow. At the same time, a person 6 ft tall casts a 4-ft shadow. Use similar triangles to find the height of the cactus.



$$\frac{\text{Height}}{\text{Shadow}} \rightarrow \frac{6}{4} = \frac{x}{9} \quad 4x = 54 \quad x = \boxed{13.5 \text{ ft}}$$

See Chapter 7 Answers to Check

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QUIZ: Radicals, Quadratic Formula, Ratios, Proportions, and Similar Figures
7.3 #s 1,2,4-19